MIND MAP: LEARNING MADE SIMPLE CHAPTER - 1

Let A and B be two sets. If every element of A is an element of B, then A is called a subset of B and written as $A \subset B$ or $B \supset A$ (read as 'A' is contained in 'B' or 'B contains A'). B is called superset of A. Note:

- 1. Every set is a subset and superset of itself.
- 2. If A is not a subset of B, we write $A \not\subset B$.
- 3. The empty set is the subset of every set.
- 4. If A is a set with n(A) = m, then no. of element A are 2ⁿ and the number of proper subsets of A are 2ⁿ-1

Eg. Let $A = \{3, 4\}$, then subsets of A are \emptyset , $\{3\}$, $\{4\}$, $\{3, 4\}$. Here, n(A) = 2 and number of subsets of $A = 2^2 = 4$.

The number of elements in a finite set is represented by n (A), known as cardinal number.

Eg.: $A = \{a, b, c, d, e\}$ Then, n(A) = 5

Set builder form or Rule Method

Representation of Sets

A set which has no element is called null set. It is denoted by symbol ϕ or $\{\}$.

E.g. Set of all real numbers whose square is -1.

In set-builder form: $\{x:x \text{ is a real number whose square is } -1\}$ In roaster form: $\{ \}$ or \emptyset

A set which has finite number of elements is called a finite set. Otherwise, it is called an infinite set.

E.g.: The set of all days in a week is a finite set whereas the set of all integers, denoted by

 $\{\ldots -2, -1, 0, 1, 2, \ldots\}$ or $\{x \mid x \text{ is an integer}\}$ is an infinite

An empty set ϕ which has no element is a finite set A is called empty or void or null set.

Two sets A and B are set to be equal, written as A=B, if every element of A is in B and every element of B is in A. e.g.: (i) $A = \{1, 2, 3, 4\}$ and $B = \{3, 1, 4, 2\}$, then A = B(ii) $A = \{x: x-5=0\}$ and $B = \{x: x \text{ is an integral positive root } \}$ of the equation $x^2 - 2x - 15 = 0$

Then A = B

SEIS

A set is collection of well-defined distinguished objects. The sets are usually denoted by capital letters A, B, C etc., and the members or elements of the set are denoted by lower case letters a, b, c etc.., If x is a member of the set A, we write $x \in A$ (read as 'x' belongs to A) and if x is not a member of set A, we write $x \notin A(\text{read as '}x' \text{ doesn't belongs})$ to A). If x and y both belong to A, we write $x, y \in A$.

Some examples of sets are: A: odd numbers less than 10

N: the set of all rational numbers

B: the vowels in the English alphabates

O: the set of all rational numbers.

In this form, we write a variable (say x) representing any member of the set followed by property satisfied by each member of the set. eg.: The set A of all prime number less than 10 in set builder form is written as

 $A = \{x \mid x \text{ is a prime number less than 10}\}$

The symbol "|" stands for the word "such that". Sometimes, we use symbol ":" in place of symbol "|"

In this form, we first list all the members of the set within braces (curly brackets) and separate these by commas.

Eg: The set of all natural number less than 10 in this form is written as: $A = \{1, 3, 5, 7, 9\}$

In roaster form, every element of the set is listed only once.

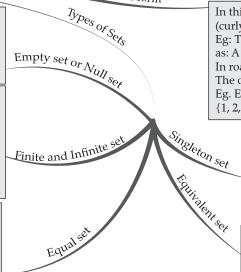
The order in which the elements are listed is immaterial.

Eg. Each of the following sets denotes the same set $\{1, 2, 3\}, \{3, 2, 1\}, \{1, 3, 2\}$

> A set having one element is called singleton set. e.g.: (i) $\{0\}$ is a singleton set, whose only member is 0. (ii) $A = \{x: 1 < x < 3, x \text{ is a natural number} \}$ is a singleton set which has only one member which is 2.

Two finite sets A and B are said to be equivalent, if n(A) = n(B). Clearly, equal set are equivalent but equivalent set need not to be equal.

e.g.: The sets $A = \{4, 5, 3, 2\}$ and $B = \{1, 6, 8, 9\}$ are equivalent, but are not equal.



Roaster or Tabular form







MIND MAP: LEARNING MADE SIMPLE CHAPTER - 1(A)

A Venn diagram is an illustration of the relationships between and among sets, groups of objects that share something common These diagrams consist of rectangle and closed curves usually

circles Eg: •1 In the given venn diagram $U = \{1,2,3,.....10\}$ universe set of which $A = \{2,4,6,8,10\}$ and $B = \{4,6\}$ are subsets and also B⊂A

- 1. For any set A, we have
- (a) $A \cup A = A$, (b) $A \cap A = A$, (c) $A \cup \phi = A$, (d) $A \cap \phi = \phi$, (e) $A \cup U = U$ (f) $A \cap U = A$, (g) $A - \phi = A$, (h) $A - A = \phi$
- 2. For any two sets A and B we have
- (a) $A \cup B = B \cup A$, (b) $A \cap B = B \cap A$, (c) $A B \subseteq A$, (d) $B A \subseteq B$
- 3. For any three sets A,B and C, we have
- (a) $A \cup (B \cup C) = (A \cup B) \cup C$, (b) $A \cap (B \cap C) = (A \cap B) \cap C$
- (c) $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$, (d) $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
- (e) $A-(B\cup C)=(A-B) \cap (A-C)$, (f) $A-(B\cap C)=(A-B)\cup (A-C)$

The union of two sets A and B, written as $A \cup B$ (read as A union B) is the set of all elements which are either in A or in B in both. Thus, $A \cup B = \{x: x \in A \text{ or } x \in B\}$

clearly, $x \in A \cup B \Rightarrow x \in A \text{ or } x \in B \text{ and } x \notin A \cup B \Rightarrow x \notin A \text{ and } x \notin B$



eg: If $A = \{a, b, c, d\}$ and $B = \{c, d, e, f\}$ then $A \cup B = \{a, b, c, d, e, f\}$

The intersection of two sets A and B, written as $A \cap B$ (read as 'A' intersection 'B') is the set consisting of all the common elements of A and B.

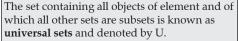
Thus, $A \cap B = \{x : x \in A \text{ and } x \in B\}$

Clearly, $x \in A \cap B \Rightarrow \{x \in A \text{ and } x \in B\}$ and $x \notin A \cap B \Rightarrow \{x \notin A \text{ or } x \in A \cap B \Rightarrow (x \notin A \cap B)\}$ ∉B}.

Eg: If $A = \{a,b,c,d\}$ and $B = \{c,d,e,f\}$ Then $A \cap B = \{c,d\}$



Two sets A and B are said to be disjoint, if $A \cap B = \emptyset$ i.e, A and B have no common element. e.g. if $A = \{1, 3, 5\}$ and $B = \{2, 4, 6\}$ Then, $A \cap B = \emptyset$, so A and B are disjoint.



E.g : For the set of all intergers, the universal set can be the set of rational numbers or the set

Difference of two sets

Universal Set

R of real numbers

The set of all subset of a given set A is called **power set** of A and denoted by P(A).

E.g : If $A = \{1,2,3,\}$, then $P(A) = \{\phi\}$, {1},{2}, {3},{1,2},{1,3},{2,3},{1,2,3} Clearly, if A has n elements, then its power set P (A) contains exactly 2ⁿ elements.

Operations on Sets

Algebra of sets

The symmetric difference of two sets

A and B, denoted by A Δ B, in defined Eg. If $A = \frac{1}{100}$, and $B = \{1,3,5,7,9\}$ then $A = \{1,3,5,7,9\}$ as $(A \triangle B) = (A-B) \cup (B-A)$

If A and B are two sets, then their difference A-B is defined as: $A-B = \{x : x \in A \text{ and } x \notin B\}$

Similarly, $B - A = \{x : x \in B \text{ and } x \notin A\}$ Eg. If $A = \{1,2,3,4,5,\}$ and $B = \{1,3,5,7,9\}$

 $A-B=\{2,4\}$ and $B-A=\{7,9\}$

SETS

Compliment of Set

 The set of natural numbers $N = \{1, 2, 3, 4, 5, ---\}$

- The set of integers $Z = \{...-3, -2, -1, 0, 1, 2, 3, ---\}$
- The set of irrational numbers, $T = \{x: x \in R \text{ and } x \in Q\}$
- The set of rational number $Q = \{x : x = \frac{p}{q}, p, q \in Z \text{ and } q \neq 0\}$ Relation among these subsets are $N \subset Z \subset O$, $O \subset R$, $T \subset R$, $N \not\subset T$

of U, then complement of A is the set which contains those elements of U. which are not present in A and is denoted by A' or A^c. Thus, $A^{c} = \{x: x \in U \text{ and } x \notin A\}$ e.g.: If $U = \{1, 2, 3, 4, ...\}$ and $A = \{2, 4, 6, 8,\}$ then $A^{c} = \{1, 3, 5, 7, ...\}$

If U is a universal set and A is a subset

Properties of complement

▼ Interval Notation

Let a and b be real numbers with a < b Region on the Set of Real Numbers Interval Notation real number line [a, b) (a, b) [a, b] $(-\infty, b)$ $(-\infty, b]$ (a, ∞) [a, ∞)

• Complement law:

- (i) $A \cup A' = U$ (ii) $A \cap A' = \phi$
- De morgan's Law:
- (i) $(A \cup B)' = A' \cap B'$ (ii) $(A \cap B)' = A' \cup B'$ Double Complement law: (A')' = A
- · Law of empty set and universal set $\phi' = U$ and $U' = \phi$



• $\{x | a < x < b\}$

 $\{x \mid a \le x < b\}$

• $\{x \mid a < x \le b\}$

 $\cdot \{x \mid a \le x \le b\}$

 $\cdot \{x \mid x < b\}$

 $\{x \mid x \leq b\}$

 $\cdot \{x \mid x > a\}$

 $\cdot \{x \mid x > a\}$

Subsets of a set of



